

# ASI-MGK: IMPLICATIVE STATISTICAL ANALYSIS TOOL BASED ON $M_{GK}$

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## **ABSTRACT**

*We propose in this paper to present a statistical analysis tool integrating some well-known algorithms for extracting optimized patterns and algorithm for extracting rules based on about forty existing interest measures in the literature, including the pruning threshold. is based on a critical value of the measure of interest  $M_{GK}$ . The tool is equipped with two results presentation windows, one in a table that can be exported in LaTeX and the other interactive dynamic display window for an implicit graph.*

## **KEYWORDS**

*Association rule mining, itemset mining, ISA, implicative graphs.*

## **1. INTRODUCTION**

Association Rule Extraction is a very important task in data mining, usually consisting of four iterative and interactive steps, namely: data processing; generation of patterns and set of candidate patterns, extraction of valid rules and visualization and interpretation of results. In the two middle steps, many existing algorithms and the properties of these algorithms have given rise to a large number of works. In the first processing step, currently there are several data formats: raw text data, csv data, araff data. These data can be coded in binary or quantitative or qualitative data and can be represented in sequences or transactions.

According to the coding and the representation of the data, the methodologies used in the second extraction step diverges; hence the existence of several pattern generation algorithms or set of patterns in the literature, each of them have the ambition to reduce the processing time and memory capacity used or even the access time to the Data Base .

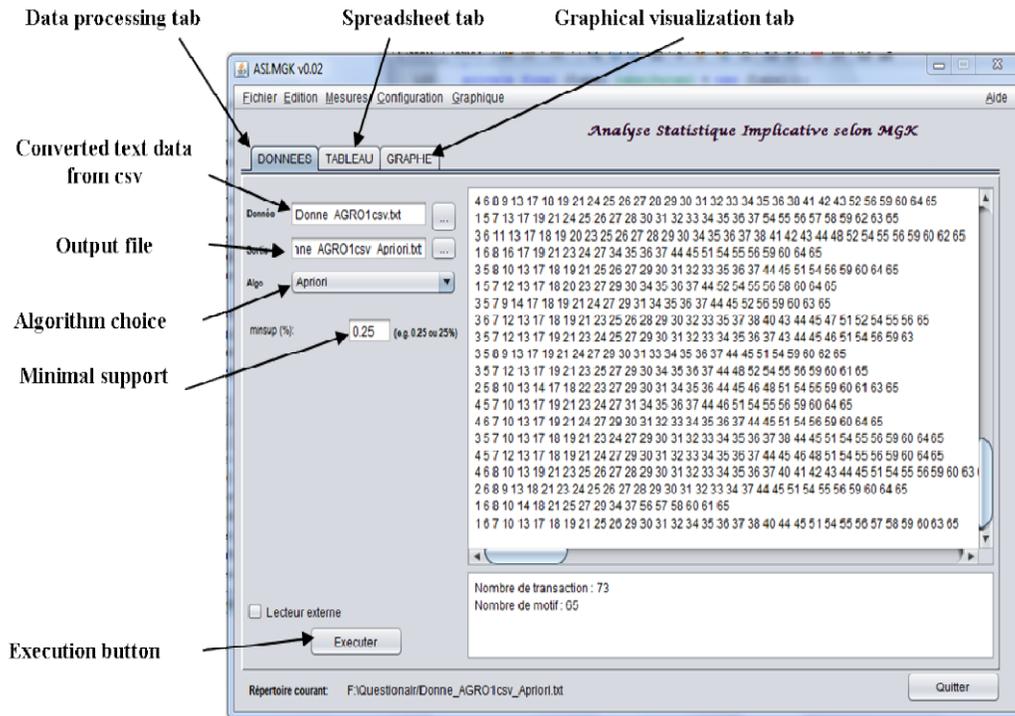
The third step, is also a very important steps. Several research centers are interested in this, it is the extraction of valid rules where the validation of the rules, often conditioned by the discriminant, the relevant, the robustness and the non-redundant. The existence of several measures of interest in the literature and the use of overdraft and optimization of rules extraction algorithm explain the divergence of ideas and the evolution of research in this field. We refer the reader to the syntheses proposed by Gras and al. (2004), Geng and Hamilton (2006), Lallich and al. (2007), Lenca and al. (2007), Geng and Hamilton (2007) and Suzuki (2008).

Several tools already implement some of these steps and their algorithms, but most of them rely on the support-trust or support-lift, or sometimes support-conviction pair. The pruning threshold is a value arbitrarily chosen as *minconf* and *minlif* for trust and lift respectively.

In ASI-MGK, we implemented the more famous algorithms and introduced some 40 measures of interest and optimized the chi-square threshold based on the  $M_{GK}$  interest measure.

## 2 ASI-MGK DESCRIPTION

Software allowing the extraction of such rules and propose to use the lift (IBM, XLSTAT, ORANGE, WEKA) in addition to support and trust. The tool Felix (Lehn, 2000) integrates the intensity of implication and its entropic version. The Herbs experimentation platform (Vaillant, 2002) integrates 20 quality measures (*support, confidence, linear correlation coefficient, centered confidence, conviction, Piatetsky-Shapiro, Loevinger, Sebag-Schoenauer information gain, lift, Laplace, less contradiction, odds multiplier, rate of examples and counterexamples, Cohen quality index, Zhang, implication index, intensity of involvement, intensity of entropic implication and discriminating probabilistic index*).

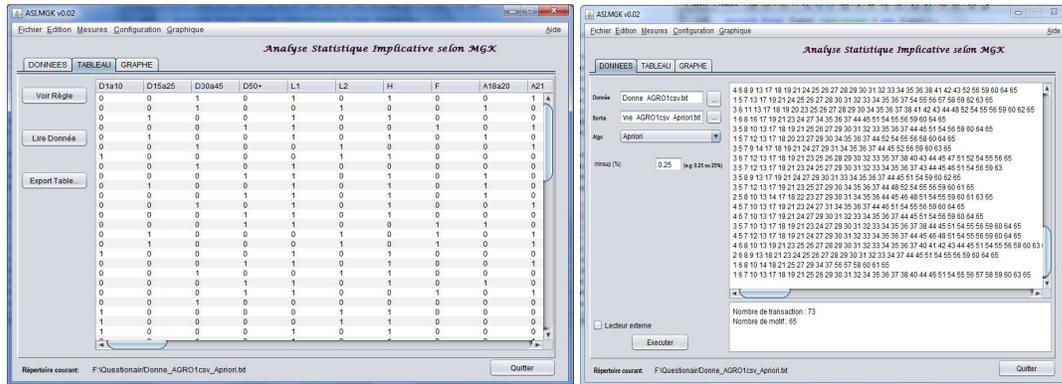


**Figure 1: ASI-MGK window**

The ASI-MGK software is a Java application (developed in Java programming language) designed to help young researchers in data analysis. More specifically, this software constitutes three tabs; The first two menus of the ASI-MGK guide the user through three stages of the association rule extraction process, using a graphical user interface: reading or data conversion, generating candidate items, or directly extracting rules. The last tab concerns the operations of analysis and visualization of the results.

## 2.1. Data reading and transformation

This is the first phase that was generally called the preprocessing phase. It consists of selecting from the database the data (attributes and objects) that are useful for extracting association rules and transforming them into data. an extraction context.



**Figure 2: ASI-MGK data view windows: on the left it is a representation in binary table and on the right it is a representation in transaction.**

This is a preliminary preparatory work to bring the data to the transactional format. In the preparation phase, the ASI-MGK offers us several algorithms; conversion algorithm: sequence in transaction, CSV in data. These possibilities will allow him to read multiple text data formats and CSV data.

## 2.2 Frequent pattern mining

An association rule extraction context is a  $B = (\mathcal{O}, I, \mathcal{R})$  triplet in which  $\mathcal{O}$  is called set of objects (or transactions),  $I$  set of attributes (or items), and  $\mathcal{R} \subseteq \mathcal{O} \times I$  is a binary relation. An association rule is a pair  $(X, Y) \in 2^I \times 2^I$  of patterns, noted:  $X \rightarrow Y$ , where  $X$  and  $Y$  are of disjoint motives ( $X, Y \subseteq I$  and  $X \cap Y = \emptyset$ ), respectively called premise and consequent of the rule. In what follows, denote by  $n = |\mathcal{O}|$  and  $P$  the uniform probability on  $(\mathcal{O}, \mathcal{P}(\mathcal{O}))$ , defined for all  $X \subseteq I$ , by:  $P(X) = \frac{n_X}{n}$ .

This phase consists of extracting from the context all sets of  $X \subseteq I$  binary attributes, called sets of elements, which are frequent in the  $Y$  context. An itemset  $X$  is common if its support is the number of objects in the context containing  $Y$ , greater than or equal to the minimum support.

Knowledge extraction processes in databases vary depending on properties and different types of data. There are several efficient algorithms for extracting frequent sets in the literature, but we chose the following tool: Apiori, Close and A-Close, Agrawal and Srikant (1994).

### 2.3 Rule extraction

Much research on the association rules extraction in data mining define several measures of interest and their properties. We refer the reader to the syntheses proposed by Totohasina and Feno. (2008), Lenca and al., (2004).

Below, in this configuration window, we present the 42 interest measures of the association rules (A.R ) used to reduce the number of valid A.R included in our ASI-MGK tools.

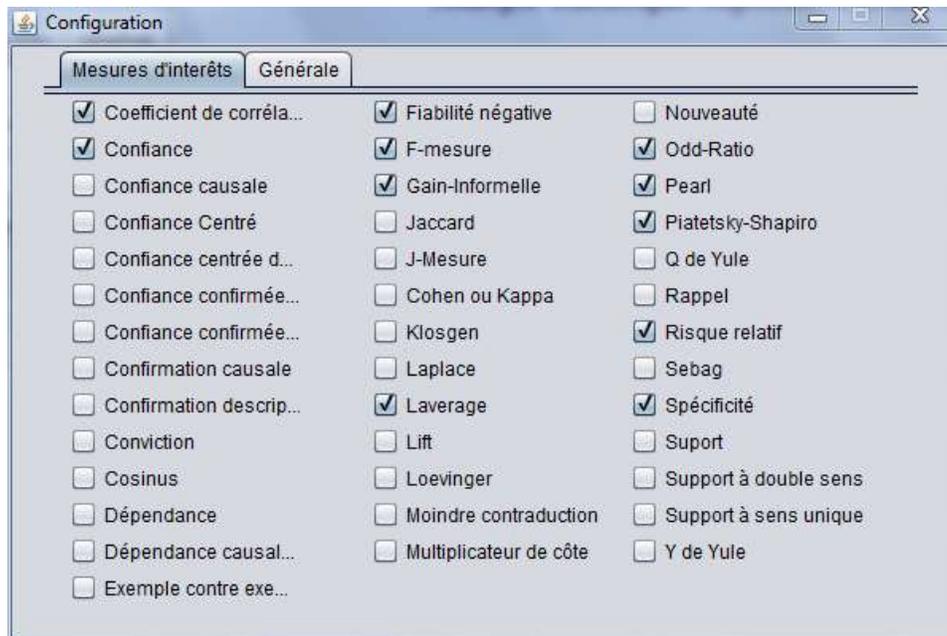


Figure 3: ASI-MGK configuration window for the interest measures to be integrated

**Definition 1.** (*Support*) Support for a  $X \rightarrow Y$  association rule is the proportion of transactions in the database that contain  $X \wedge Y$ .  $supp(X \rightarrow Y) = P(X' \cap Y')$

A rule  $r: X \rightarrow Y$  is valid according to support if  $supp(X \rightarrow Y) \geq minsup$ .

Studies on rule quality measures have been completed; Feno in his thesis in 2007 has characterized a basis for valid association rules in the sense of the  $M_{GK}$  quality measure. According to the eligibility criteria, Totohasina in its PhD thesis 2008 has confirmed that the use of this quality measure overcomes the problems of methods of the extraction of association rules using the quality measures Confidence.

Thus we chose the measures of interest denominated Confidence of Guillaume noted ConfG or measures called Guillaume-Kenchaff abbreviated  $M_{GK}$ , Implication oriented standardized abbreviated *ION*, conditional probability incremental ratio or *CPIR*.

**Definition 2.** ( $M_{GK}$ ) Let  $X$  and  $Y$  be two reasons for a data mining context. We define the measure  $M_{GK}$  by: (Guillaume, 2000)

$$M_{GK}(X \rightarrow Y) = \begin{cases} \frac{P(Y|X) - P(Y)}{1 - P(Y)}, & \text{if } P(Y|X) \geq P(Y); \\ \frac{P(Y|X) - P(Y)}{P(Y)}, & \text{if } P(Y|X) < P(Y). \end{cases} \quad (1)$$

The main mathematical properties characterizing this measure of quality are developed in (Feno and Totohasina 2007), we invite the interested reader to consult them in their works.

**Definition 3.** A rule  $X \rightarrow Y$  is potentially interesting, if the support of its premise is inferior to that of its consequence.

**Definition 4.** Let  $X$  and  $Y$  be two patterns such that  $P(Y|X) \geq P(Y)$  and  $P(X) \leq P(Y)$ , then  $M_{GK}(Y \rightarrow X) \leq M_{GK}(X \rightarrow Y)$

**Definition 5.** Given a minimal threshold *minsupp* for the measure of support and error risk  $\alpha$  for  $M_{GKcr}$ , the set  $\mathcal{R}$  of valid rules is:

$$\mathcal{R} = \{(X, Y) \subseteq I \times I \mid \text{supp}(X \rightarrow Y) \geq \text{minsupp} \text{ and } M_{GK}(X \rightarrow Y) \geq M_{GKcr}(X \rightarrow Y, \alpha)\}$$

Given a  $\mathcal{B}$  database of  $n$  transactions, where  $n_X$  and  $n_Y$  are supports of the patterns  $X$  and  $Y$  respectively. The critical value  $M_{GKcr}$  for the measure  $M_{GK}$ , proposed in (Totohasina and Feno),

is obtained in the following way. Consider a contingency table by crossing these two patterns  $X$  and  $Y$ , using critical value of Pearson's chi-square ( $\chi_{cr}^2$ ) statistic with one degree of freedom, such as:

$$M_{GKcr}(X \rightarrow Y, \alpha) = \sqrt{\frac{1}{n} \frac{n-n_X}{n_X} \frac{n_Y}{n-n_Y} \chi_{cr}^2(\alpha)}, \text{ if } X \text{ favors } Y. \quad (2)$$

From the table of  $\chi^2$ , this relation makes it possible to easily develop the abacuses of the critical values of  $M_{GK}$  to decide its meaning towards an association rule.

## 2.4 Results analysis and visualization

This phase consists in the visualization by the user of the association rules extracted from the context and their interpretation in order to deduce useful knowledge for the improvement of the activity concerned.

In this step our **ASI-MGK** tool offer three result presentation registers:

1. open text format representation, save in ASCII text format, the rules are printed in tabular data as tab-separated values (fig 4).
2. Interactive dynamic table, where the user can filter and sort the extracted association rules as needed.
3. Interactive dynamic implicative graph (fig 5), on which the user can reorganize the graph and move or even delete the vertices (items). The properties of the generated graph can be:
  - a directed digraph (between two items given  $X \rightarrow Y$  and  $Y \rightarrow X$  can all be validated).
  - a bi-valued graph (the arcs can carry two value of measure of interest:  $M_{GK}$  and a interest measures previously chosen to compare with  $M_{GK}$ ).

Antécédent	Conséquence	Confiance	MGK	Couverture	Prévalence
TravTerre	Chgmt	0.88	0.52	0.7	0.75
DR.Com	DR.Agr1	0.88	0.75	0.47	0.53
Act.Dvpt	Sup.TP	0.98	0.88	0.58	0.81
TecInov	ColPltNou	0.84	0.63	0.52	0.58
Act.Dvpt	ColPltNou	0.79	0.5	0.58	0.58
ColPltNou	Act.Dvpt	0.79	0.5	0.58	0.58
TecInov	Act.Dvpt	0.87	0.69	0.52	0.58
Chgmt	Sup.Pro.Imp	0.89	0.53	0.75	0.77
TerrPr	PsbCulterr	0.97	0.91	0.52	0.71
PVTerrPr	PsbCulterr	0.87	0.55	0.63	0.71
PsbCulterr	Garabien	0.88	0.53	0.71	0.75
TerrPr	PVTerrPr	0.95	0.86	0.52	0.63
TerrPr	Garabien	0.92	0.68	0.52	0.75
PVTerrPr	Garabien	0.89	0.56	0.63	0.75
JurISecr	Garabien	0.94	0.77	0.48	0.75
SojaInfli	SojaAPouv	0.95	0.63	0.81	0.86

Figure 4: Associations rules extracted in text format

Visualizations based on implicative graphs quickly show their limits when the number of rules is important: the arcs intersect very often and the abundance of nodes and arcs leads to occlusion.

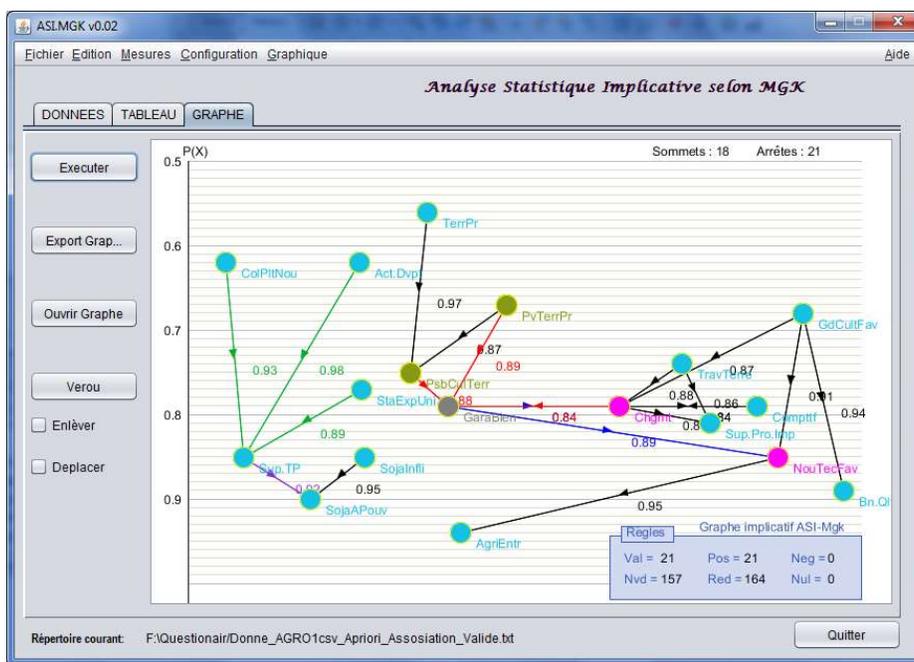
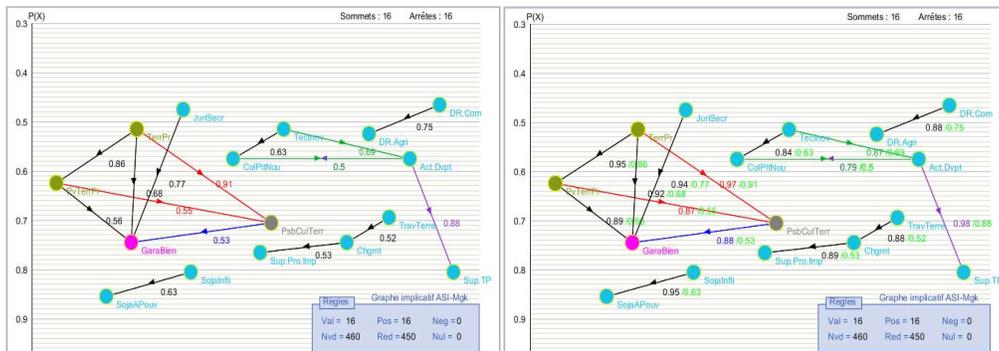


Figure 5: ASI-MGK interactive dynamic implicative graph viewer.



**Figure 6: The implicative graphs displayed in the graphical window of the ASI-MGK: on the left a simple graph and on the right a bivalued digraph.**

## 2.5 Results analysis

Here is the report of the processing of the ASI-MGK software, a data set of a survey conducted at L2 agronomy student, containing 74 transactions and 65 attributes.

```

===== STATISTIQUES APRIORI =====
Candidates number: 703 The algorithm is stopped at size 2
Frequent items number: 500
Maximum memory used : 13.183204650878906 mb
Total time ~ 0 ms
===== STATS DE GENERATION DES REGLES =====
Valid association rules number generated : 16
Discarded : 910
Redundant rules number: 450
Invalid rules : 460 Rate : 0.03
Error risk : 0.001
Total time ~ 1326 ms
    
```

The main line of this result (fig 4) corresponds to this:

TravTerre Chgmt 0.88 0.52 0.7 0.75

It is interpreted as follows: The support of the premise is  $\text{supp}(\text{TravTerre})=0.7$  and that of consequence is  $\text{supp}(\text{Chgmt}) = 0.75$ .

According to the interest measure confidence, the rule R1:(TravTerre -> Chgmt) is valid because

$\text{conf}(\text{TravTerre} \rightarrow \text{Chgmt}) = 0.88$  .

According to our approach (Def. 5)  $\text{Supp}(\text{TravTerre}) < \text{Supp}(\text{Chgmt})$  that is to say  $R1:(\text{TravTerre} \rightarrow \text{Chgmt})$  is potentially interesting, we can evaluate  $\text{MGK}(\text{TravTerre} \rightarrow \text{Chgmt}) = 0.52$   
 $0.52 > \text{MGKcr}(\text{TravTerre} \rightarrow \text{Chgmt}, 0.001) = 0.44$  .  
So the rule  $R1:(\text{TravTerre} \rightarrow \text{Chgmt})$  is also valid in the sense of  $M_{GK}$ .

### 3 CONCLUSION

In summary, we presented an implicit statistical analysis tool incorporating algorithms to extract knowledge from a binary database. In addition, we have also implemented and optimized the relevant algorithms. The specificity of this tool, among others, is that the proposed tool uses the quality measure of association rules  $M_{GK}$ . Presumably, the advantage of this approach lies in the use of  $M_{GK}$ , which is non-symmetric and implicative, and in the fact that the threshold is determined objectively from a chi-square independence test. We can therefore trust the results obtained if the risk defined by the user is very low. Is not it more motivating to use an application giving reliable results?

As future work, we will integrate the implicative cohesion and classification (Rakotomalala and al 2017) part in ASI-MGK and then we will present the procedure of the complete data processing following all the steps of the data mining with real data using this tool.

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